

## Issues in Standard Cosmology

$$\chi = \int_c^0 \frac{dt}{a} = \int_c^0 \frac{dln a}{aH} = \int_c^0 \frac{dz}{H}$$

$$-dt = a dr$$

$$dln a = -dln c(t+z) = H dt$$

\* particle horizon  $\chi_h = \chi(t_0=0)$

for convergence of  $a \rightarrow 0$ .  $aH \propto \sqrt{9a^2 - K} \sim a^n$

$$n < 0$$

$\therefore$  ok for mde, rde, but no  $\Lambda$ de

$$* S \sim a^n, a \sim t^{2/n}$$

$$\chi \sim [t^{-\frac{n+1}{2}}]_{t_i}^{t_f}$$

$$* S \sim \Lambda, a \sim e^{Ht}$$

$$\chi \sim [\frac{1}{H} e^{-Ht}]_{t_i}^{t_f}$$

\* event horizon  $\chi_e = \chi(t_0 \rightarrow \infty)$

Yes for  $\Lambda$ de = closed, but no for flat or open

## Horizon problem

$$\text{mde } \chi = 6000^+ \text{ Mpc } (1+z)^{1/2} \rightarrow \chi_h(z=1100) \sim (80 h^+ \text{ Mpc})$$

$$\text{comoving distance } r \text{ to } z=1100 \rightarrow r = \int_0^z \frac{dz}{H} \sim 5820 h^+ \text{ Mpc}$$

$$\rightarrow \theta \approx 1.8 \text{ degree} \approx 0.031$$

no time for communication

## Flatness problem

$$\Omega_{\text{tot}} = \Omega_m + \Omega_r + \Omega_\Lambda + \dots \quad \text{without } \Omega_\Lambda$$

$$H^2 = \frac{8\pi G}{3} \rho - \frac{K}{a^2} \rightarrow -\frac{3K}{8\pi G \rho a^2} = \frac{3H^2}{8\pi G \rho} - 1 = \Omega_{\text{tot}} - 1$$

today the deviation from unity  $\Omega_{\text{tot}} - 1 \approx 10$

but smaller by  $10^{-60}$

( $K=0$  solved)

$$\rightarrow \frac{\Omega_{\text{tot}}(t_p) - 1}{\Omega_{\text{tot}}(t_0) - 1} = \frac{(\rho a^2)_{t_0}}{(\rho a^2)_{t_i}} \frac{(\rho a^2)_{t_0}}{(\rho a^2)_{t_f}}$$

$$\sim \frac{T_0}{T_{\text{ee}}} \left( \frac{T_{\text{ee}}}{T_{\text{pi}}} \right)^2 \sim 10^{-60}$$

## Monopole Problem (real problem?)

$T_{GUT} \sim 10^{16-15}$  GeV . topological defects from phase transition  
typically one defect per horizon at GUT  $\rightarrow \rho_{today} \sim T_{GUT}^4 \rightarrow 10^{10}$

$$E_0 \sim 10^{-9}$$

## Structure formation problem

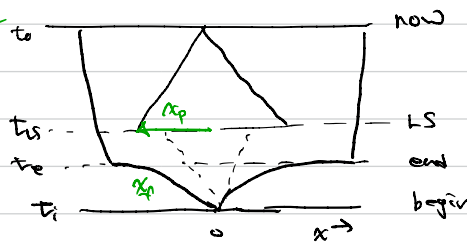
clusters of galaxies  $M \sim 10^{15} M_\odot$  .  $R \sim 10$  Mpc comoving .  $E_{grav} \sim 10^{-5}$  per unit proton mass  
should be in causal contact to collapse gravitationally  $\rightarrow R < x_h \rightarrow$  only  $z < 10^6$  (or BBN)  
but nothing in standard after BBN generates inhomogeneities of such high binding  $E$ .

$\Rightarrow$  can be assumed as weird initial conditions

## Inflation : accelerated expansion

$$x_p = \int_{t_i}^{t_0} \frac{dt}{a} \sim 3t_0 \quad \text{MDE}$$

$$x_p = \int_{t_i}^{t_f} \frac{dt}{a} = \frac{1}{a_0 H_{inf}} \left[ e^{H_{inf} t} \right] \quad a = a_0 e^{H_{inf}(t-t_0)}$$



comoving horizon  
 $\sim \frac{1}{aH}$  decrease  
 $\leftrightarrow$  larger in the past  
 $\frac{d}{dt} \left( \frac{1}{aH} \right) < 0$

$$x_p \gg x_h \Rightarrow e^{H_{inf} t_0} > a_0 H_{inf} \cdot 3t_0 \sim \frac{T_0}{T_e} = 10^{26} \left( \frac{T_e}{10^{16} \text{ GeV}} \right) \Rightarrow H_{inf} t_0 \geq 2 \ln 10 \approx 60$$

$$* \frac{\Sigma_i^2 - 1}{\Sigma_i^2 + 1} = \frac{(\Sigma_i^2)_e}{(\Sigma_i^2)_i} = \frac{a_i^2}{a_e^2} \geq (10^{26})^2 = 10^{52}$$

flatness problem  
mitigated by expansion

$$\delta t \geq 10^{-33} \text{ sec}$$

$$* \text{scale for monopole} \sim \frac{1}{a^2} \sim e^{-2H_{inf} t}$$

60 e-folding

## Requirement

- \* has to end. ( $\Lambda$ : cannot)
- \* with large expansion.  $T \rightarrow 0$  for ordinary radiation, if any.
  - $\rightarrow$  reheating: needed to produce ordinary matter. inflaton gone
  - hot enough for baryogenesis, but smooth enough for no monopole or defects

## Models

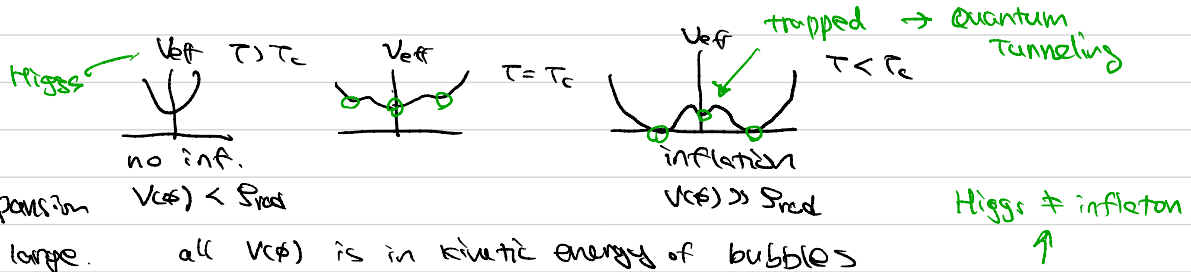
- \* Old by Guth (original)

### graceful exit problem

true vacuum: ordinary expansion

false vacuum: inflation  $\rightarrow$  large.

they have to collide to release the energy & stop  $\rightarrow$  too much inhomogeneities



- \* New by Linde, Steinhardt (similar but

smooth 2nd-order phase transition, but slow-roll  $\rightarrow$  minima  $\gg M_{Pl}$  unnatural.

also  $\phi_{ini}$  should be  $\ll M_{Pl}$  otherwise stops too early  $\rightarrow$  fine-tuning.



- \* chaotic by Linde:  $V = \frac{1}{2} m_p^2 \phi^2$ .

chaotically some region satisfies  $V \gg S$ . slow-motion  $\rightarrow$  this region inflates  $\rightarrow$  our univ.

(other regions x) But this requires  $\phi_{ini} \gg M_{Pl}$ . Quantum grav?